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# Structure of a new high-pressure-high-temperature modification of antimony(III) oxide, $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$, from high-resolution synchrotron powder diffraction data 

A quenchable new high-pressure-high-temperature modification of antimony(III) oxide, $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$, has been obtained at hydrostatic pressures of $9-11 \mathrm{GPa}$ and temperatures of 573773 K . Its crystal structure has been determined from highresolution synchrotron powder diffraction data. $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ consists of three-dimensionally cross-linked infinite chains of $\mathrm{SbO}_{3} E$ units ( $E=$ lone pair) with the chains forming tetragonal rod-packing. The underlying topology of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}(3,3 \mathrm{~T} 8)$ is found very rarely in inorganic structures; it is realised only for the polyanion $\left[\mathrm{Si}_{4} \mathrm{O}_{4} \mathrm{~N}_{6}\right]^{10-}$ that occurs in the $\mathrm{Ce}_{4}\left(\mathrm{Si}_{4} \mathrm{O}_{4} \mathrm{~N}_{6}\right) \mathrm{O}$ structure type. The structural relation to the two previously known polymorphs of $\mathrm{Sb}_{2} \mathrm{O}_{3}$ at ambient pressure, valentinite and senarmontite is discussed.

## 1. Introduction

In the system antimony-oxygen four different oxides, $\mathrm{Sb}_{2} \mathrm{O}_{3}$ (Dehlinger \& Glocker, 1927; Bozorth, 1923; Svensson, 1974, 1975; Manohar \& Gopalakrishnan, 1975; White et al., 1967; Fenwick \& Roberts, 1928; Hendricks \& Burger, 1937), $\mathrm{Sb}_{2} \mathrm{O}_{4}$ (Pätzold et al., 1962; Dihlström, 1938; Thornton, 1977; Monge et al., 1988), $\mathrm{Sb}_{6} \mathrm{O}_{13}$ (Stewart et al., 1972) and $\mathrm{Sb}_{2} \mathrm{O}_{5}$ (Dehlinger, 1927; Jansen, 1978, 1979), are known to exist at ambient pressure ( $p=1 \mathrm{bar}$ ) and temperatures up to $T=$ 1523 K . For $\mathrm{Sb}_{2} \mathrm{O}_{3}$ two modifications have been reported: cubic $\alpha-\mathrm{Sb}_{2} \mathrm{O}_{3}$ (senarmontite; Fig. 1) and orthorhombic $\beta$ -


Figure 1
Packing diagram of senarmontite $\left(\alpha-\mathrm{Sb}_{2} \mathrm{O}_{3}\right)$ in $F d \overline{3} m$ under ambient conditions in a perspective view along the $c$ axis.

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Table 1
Crystallographic and Rietveld refinement data for $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ at ambient conditions.

Crystal data
Chemical formula
$M_{\mathrm{r}}$
Crystal data, space group
Temperature (K)
$a, b, c(\AA)$
$V\left(\AA^{3}\right)$
Z
Radiation type
Specimen shape
Data collection
Diffractometer
Specimen mounting
Data collection mode
Scan method
$2 \theta$ values $\left({ }^{\circ}\right)$

Refinement
$R$ factors and goodness of fit
Time/scan (h)
No. of data points
No. of parameters
No. of restraints

```
Sb}\mp@subsup{\mp@code{O}}{3}{
291.50
Orthorhombic, P2 2 2, 2,
298
11.6411 (1), 7.5666 (0), 7.4771 (0)
658.61 (1)
8
Synchrotron, }\lambda=0.24804 
White powder
Multi-analyser stage
0.3 mm capillary
Continuous mode with rebinning Debye-Scherer
```



```
    0.002
```

$R_{\mathrm{p}}=0.043, R_{\mathrm{wp}}=0.067, R_{\exp }=0.021$,
$\chi^{2}=3.245$
1
12420
82
0
$\mathrm{Sb}_{2} \mathrm{O}_{3}$ (valentinite; Fig. 2). $\alpha$ - $\mathrm{Sb}_{2} \mathrm{O}_{3}$ crystallizes in $\mathrm{Fd} 3 m$ (No. 227) with $a=11.1519 \AA, V=1386.91 \AA^{3}$ and $Z=16$ (Bozorth, 1923; Svensson, 1975), is isotypic with cubic $\mathrm{As}_{2} \mathrm{O}_{3}$, and is stable at ambient conditions, while $\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}$ Pccn (No. 56) with $a=4.911, b=12.464, c=5.412 \AA, V=331.27 \AA^{3}$ and $Z=4$ (Svensson, 1974), is reported to exist at high temperature. According to the literature (Manohar \& Gopalakrishnan, 1975; White et al., 1967; Fenwick \& Roberts, 1928; Hendricks


Figure 2
Packing diagram of valentinite $\left(\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}\right)$ in Pccn under ambient conditions in a perspective view along the $a$ axis.
\& Burger, 1937), the phase transition from $\alpha$ - towards $\beta$ - $\mathrm{Sb}_{2} \mathrm{O}_{3}$ occurs at a temperature between 843 and 879 K . Although $\beta$ $\mathrm{Sb}_{2} \mathrm{O}_{3}$ is metastable, it can exist for extended periods of time under ambient conditions (Manohar \& Gopalakrishnan, 1975; Hendricks \& Burger, 1937). $\mathrm{Sb}_{2} \mathrm{O}_{3}$ was investigated at hydrothermal conditions in the range up to $p=0.3 \mathrm{GPa}$ and $T=973 \mathrm{~K}$, but no new phases were found (White et al., 1967). Since antimony(III) expresses a stereochemically active lone pair, which results in rather open structures for both known modifications of $\mathrm{Sb}_{2} \mathrm{O}_{3}$, the compound should be susceptible to pressure-driven phase transitions, as observed already for $\mathrm{Pb}_{3} \mathrm{O}_{4}$ (Dinnebier et al., 2003), $\mathrm{SeO}_{2}$ (Stahl et al., 1992; Orosel et al., 2004) or $\mathrm{Bi}_{2} \mathrm{O}_{3}$ (Sillen, 1941; Ghedia et al., 2010). Here we report on studies using large-volume hydrostatic presses.

## 2. Experimental

### 2.1. Synthesis of the $\mathrm{Sb}_{2} \mathrm{O}_{3}$ polymorphs

Both modifications of $\mathrm{Sb}_{2} \mathrm{O}_{3}$ were used for the experiments. Commercially available $\alpha-\mathrm{Sb}_{2} \mathrm{O}_{3}$ (Alfa Aesar 99.9\%) was purified by sublimation in vacuum for 12 h applying a temperature gradient of 773 K to room temperature. $\beta$ - $\mathrm{Sb}_{2} \mathrm{O}_{3}$ was synthesized according to the literature (Debray, 1866) by combining an HCl acid solution of $\mathrm{SbCl}_{3}$ and a boiling $\mathrm{Na}_{2} \mathrm{CO}_{3}$ solution. The precipitate was dried at 373 K for 20 h . For both modifications, phase purity was confirmed by laboratory X-ray powder diffraction. After the drying process, both samples were filled into tightly sealed crucibles in an argon-filled glovebox. These crucibles were subjected to high pressure and high temperature in different presses (a piston cylinder press for pressures up to 2 GPa , a belt press for pressures up to 7 GPa , and a multianvil press for pressures higher than 7 GPa ). At pressures between 10 and 12.5 GPa , and a temperature of 673 K , a new modification of $\mathrm{Sb}_{2} \mathrm{O}_{3}$ was found which is designated $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ in the following.

### 2.2. Powder diffraction and crystal structure determination

For crystal structure determination the powder diffraction data of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$, synthesized at $p=10 \mathrm{GPa}$ and $T=673 \mathrm{~K}$, were collected at the high-resolution powder diffractometer at ID31 at the European Synchrotron Radiation Facility (ESRF) (Fig. 3). An Si (111) reflection was used to select an X-ray energy of 50 keV . The size of the beam was adjusted to $2 \times$ $0.6 \mathrm{~mm}^{2}$ using slits. The wavelength was determined to be 0.24804 (1) $\AA$ from a silicon standard. A sample of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ was contained in a 0.3 mm lithium borate glass capillary, and was rotated around $\theta$ in order to improve the randomization of the crystallites. The diffracted beam was analysed with a ninecrystal analyser stage [nine Ge (111) crystals separated by $2^{\circ}$ intervals] and detected with nine $\mathrm{Na}(\mathrm{Tl}) \mathrm{I}$ scintillation counters simultaneously. The incoming beam was monitored by an ion chamber for normalization of the decay of the primary beam. Scans were taken every 15 min at $T=298 \mathrm{~K}$ in continuous mode for 1 h . They were later normalized and converted to step scan data for values of $2 \theta$ from 1.0 to $25.84^{\circ}$ in steps of $0.002^{\circ}$. The powder pattern contains a secondary phase which

Table 2
Selected bond distances ( $\AA$ ) and angles $\left({ }^{\circ}\right)$ of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ at ambient conditions

| $\mathrm{Sb} 1-\mathrm{O} 2$ | $1.88(2)$ | $\mathrm{Sb} 3-\mathrm{O} 4$ | $2.04(1)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{Sb} 1-\mathrm{O} 5$ | $2.05(2)$ | $\mathrm{Sb} 3-\mathrm{O} 3$ | $2.04(2)$ |
| $\mathrm{Sb} 1-\mathrm{O} 1$ | $2.24(2)$ | $\mathrm{Sb} 3-\mathrm{O} 2$ | $2.11(2)$ |
| $\mathrm{Sb} 1-\mathrm{O} 2$ | $2.72(2)$ | $\mathrm{Sb} 3-\mathrm{O} 3$ | $2.52(2)$ |
| $\mathrm{Sb} 1-\mathrm{O} 1$ | $3.08(2)$ | $\mathrm{Sb} 3-\mathrm{O} 5$ | $3.17(2)$ |
| $\mathrm{Sb} 1-\mathrm{O} 4$ | $3.34(2)$ | $\mathrm{Sb} 3-\mathrm{O} 2$ | $3.18(2)$ |
| $\mathrm{Sb} 2-\mathrm{O} 1$ | $1.87(2)$ | $\mathrm{Sb} 4-\mathrm{O} 6$ | $2.00(2)$ |
| $\mathrm{Sb} 2-\mathrm{O} 4$ | $1.91(1)$ | $\mathrm{Sb} 4-\mathrm{O} 5$ | $2.06(2)$ |
| $\mathrm{Sb} 2-\mathrm{O} 6$ | $2.06(2)$ | $\mathrm{Sb} 4-\mathrm{O} 3$ | $2.08(2)$ |
| $\mathrm{Sb} 2-\mathrm{O} 1$ | $2.66(2)$ | $\mathrm{Sb} 4-\mathrm{O} 6$ | $2.59(2)$ |
| $\mathrm{Sb} 2-\mathrm{O} 5$ | $2.91(2)$ | $\mathrm{Sb} 4-\mathrm{O} 3$ | $3.03(2)$ |
| $\mathrm{Sb} 2-\mathrm{O} 6$ | $3.19(2)$ | $\mathrm{Sb} 4-\mathrm{O} 4$ | $3.32(2)$ |
|  |  |  |  |
| $\mathrm{O} 2-\mathrm{Sb} 1-\mathrm{O} 5$ | $105.2(7)$ | $\mathrm{O} 6-\mathrm{Sb} 4-\mathrm{O} 5$ | $98.4(6)$ |
| $\mathrm{O} 2-\mathrm{Sb} 1-\mathrm{O} 1$ | $101.9(7)$ | $\mathrm{O} 6-\mathrm{Sb} 4-\mathrm{O} 3$ | $95.7(7)$ |
| $\mathrm{O} 5-\mathrm{Sb} 1-\mathrm{O} 1$ | $82.6(6)$ | $\mathrm{O} 5-\mathrm{Sb} 4-\mathrm{O} 3$ | $82.4(6)$ |
| $\mathrm{O} 1-\mathrm{Sb} 2-\mathrm{O} 4$ | $105.7(6)$ | $\mathrm{Sb} 2-\mathrm{O} 1-\mathrm{Sb} 1$ | $111.3(7)$ |
| $\mathrm{O} 1-\mathrm{Sb} 2-\mathrm{O} 6$ | $88.8(7)$ | $\mathrm{Sb} 1-\mathrm{O} 2-\mathrm{Sb} 3$ | $128.1(8)$ |
| $\mathrm{O} 4-\mathrm{Sb} 2-\mathrm{O} 6$ | $99.2(7)$ | $\mathrm{Sb} 3-\mathrm{O} 3-\mathrm{Sb} 4$ | $125.8(8)$ |
| $\mathrm{O} 4-\mathrm{Sb} 3-\mathrm{O} 3$ | $88.5(5)$ | $\mathrm{Sb} 2-\mathrm{O} 4-\mathrm{Sb} 3$ | $133.6(8)$ |
| $\mathrm{O} 4-\mathrm{Sb} 3-\mathrm{O} 2$ | $93.9(6)$ | $\mathrm{Sb} 1-\mathrm{O} 5-\mathrm{Sb} 4$ | $125.2(7)$ |
| $\mathrm{O} 3-\mathrm{Sb} 3-\mathrm{O} 2$ | $90.8(6)$ | $\mathrm{Sb} 4-\mathrm{O} 6-\mathrm{Sb} 2$ | $131.6(9)$ |

could be clearly distinguished by the much broader peak width. Further experimental details are given in Table 1.

Indexing (Coelho, 2003) led to a primitive orthorhombic unit cell with lattice parameters as given in Table 1. The number of formula units per unit cell could be determined to be $Z=8$ from volume increments. The extinctions found in the powder patterns indicated $P 2_{1} 2_{1} 2_{1}$ as the most probable space group, which could later be confirmed by Rietveld refinement (Rietveld, 1969). The peak profiles and precise lattice para-


Figure 3
Scattered X-ray intensities of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ under ambient conditions as a function of diffraction angle $2 \theta$. The observed pattern (diamonds) measured in Debye-Scherrer geometry, the best Rietveld fit profiles (line) and the difference curve between the observed and the calculated profiles (below) are shown. The highangle part starting at $9.5^{\circ} 2 \theta$ is enlarged for clarity. The second phase is included as a LeBail fit.

meters were determined by a LeBail fit (LeBail et al., 1988) using the fundamental parameter approach of TOPAS Version. 4.1 (Bruker AXS, 2007; Cheary et al., 2005; Coelho, 2000). From the difference curve, the powder pattern of the impurity phase was clearly visible. Nevertheless, all attempts to index the impurity phase unambiguously failed. The indexing with the highest agreement factor, describing most of the reflections, was a monoclinic unit cell in the space group $P 2_{1} / a$ with lattice parameters of $a=11.2745$ (2), $b=5.6403$ (2), $c=9.3328(2) \AA, \beta=112.448(1)^{\circ}$ and $V=548.52(3) \AA^{3}$.

Structure determination of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ was performed using the program Endeavour, Version 1.4 (Crystal Impact GbR, 2000-2006), which combines global optimization of the difference between the calculated and measured diffraction pattern and of the potential energy of the system (Putz et al., 1999).

A subsequent Rietveld refinement using TOPAS converged to a Bragg $R$ value of 0.016 . The second phase was included in the form of a Le Bail fit. Diffraction peaks in both powder patterns showed pronounced anisotropic line broadening, which was described using the phenomenological microstrain model (Stephens, 1999). Agreement factors ( $R$ values) are listed in Table 1, and a selection of the bond distances and angles is given in Table 2. Using the programs PLATON (Spek, 2003) and K-plot (Hundt et al., 2006), no additional symmetry could be detected. The structure was also analysed using the programs MAPLE (Hoppe, 1979) and TOPOS (Blatov, 2006).

Further details on the crystal structure investigations may be obtained from the Fachinformationszentrum Karlsruhe, 76344 Eggenstein-Leopoldshafen, Germany [fax: (+49) 7247-808-666; e-mail: crysdata@fizkarlsruhe.de], on quoting the depository number CSD-414463.

## 3. Results and discussion

### 3.1. High-pressure experiments

The results of the high-pressure experiments of $\mathrm{Sb}_{2} \mathrm{O}_{3}$ are summarized in Fig. 4. Cubic $\alpha-\mathrm{Sb}_{2} \mathrm{O}_{3}$ is stable at ambient pressure until $T \simeq 873 \mathrm{~K}$, at $p=2 \mathrm{GPa}$ until $T \simeq$ 673 K and at $p=15 \mathrm{GPa}$ until $T \simeq$ 473 K. Outside these limits it transforms to orthorhombic $\beta$ $\mathrm{Sb}_{2} \mathrm{O}_{3}$ which stays stable up to $p=$ 7 GPa and $T=673 \mathrm{~K}$. At $p=7 \mathrm{GPa}$, but higher temperature, $\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}$ disproportionates to $\beta-\mathrm{Sb}_{2} \mathrm{O}_{4}$ and elemental antimony. The decomposition depends strongly on the holding time. At pressures $10 \leq p \leq$ 12.5 GPa and a temperature of $T=$ 673 K , a new modification of $\mathrm{Sb}_{2} \mathrm{O}_{3}$, called $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$, was found. A


Figure 4
Phase analysis results of high $T$-high $p$ preparations in the antimonyoxygen system under ambient conditions up to a temperature of 873 K and a pressure of 19.5 GPa .


Figure 5
Packing diagram of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ at ambient conditions in a perspective view (a) along the $a$ axis and (b) along the $b$ axis.


Figure 6
The four different $\mathrm{SbO}_{3}$ trigonal pyramids (a) or $\mathrm{SbO}_{3} E$ tetrahedra (b) of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ and their connectivity forming a helical chain along the $a$ axis at ambient conditions in a perspective view. The connections to neighboring chains are indicated by dashed lines.
second yet unknown phase was identified as a minor phase at pressures $p \simeq 10 \mathrm{GPa}$ and a major phase at a pressure of 15 GPa and a temperature of 663 K .

### 3.2. Crystal structure

The crystal structure of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ obtained at $p / T$ conditions of 10 GPa and 673 K (Fig. 5) displays a connectivity which has not been encountered in oxides thus far. Its basic principle can be expressed by the Niggli formula $\mathrm{ESbO}_{3 / 2}$, describing the coordination of antimony as a trigonal pyramid which is completed to a tetrahedron $\mathrm{SbO}_{3} E$ by considering the free electron pair ( $E=5 \mathrm{~s}^{2}$ ) as a pseudo-ligand. These primary building units are linked by sharing corners to form a threedimensional framework. However, the characterization of the coordination sphere of antimony given above is very much an approximation. Using the program package TOPOS (Blatov, 2006), one can distinguish three different levels of $\mathrm{Sb}-\mathrm{O}$ bonding corresponding to different levels of solid angles of faces of the Sb Voronoi polyhedra: 5.66, 12.77 and $17.54 \%$ of $4 \pi$ steradian, or of $\mathrm{Sb}-\mathrm{O}$ length $3.19,2.66$ and $2.24 \AA$, respectively (see the supplementary material ${ }^{\mathbf{1}}$ ). The last level of the strongest bonding conforms to the trigonal-pyramidal coordination of antimony, while the other two levels describe weaker $\mathrm{Sb} \cdots \mathrm{O}$ interactions that are discussed below.

From Figs. 6 and 7, which show the elementary repetition unit of the three-dimensional network, one identifies cyclic secondary building units (SBU) consisting of three $\mathrm{Sb}(1,2,3) \mathrm{O}_{3} E$ pseudo-tetrahedral units. These SBUs are linked to chains by primary $\mathrm{Sb}(4) \mathrm{O}_{3} E$ units, whereas two of the linking O atoms from both primary and secondary building units are involved. The remaining third oxygen atom (O3)

[^0]interlinks the resulting chains to the three-dimensional network as shown in Fig. 5.

With the TOPOS simplification procedures the O atoms can be contracted (transformed to edges) to obtain the underlying net (Alexandrov et al., 2011), which describes the structure topology in the simplest way as a net of the antimony coordination centres (Fig. 8 top). The topology of the underlying net is known under the name $3,3 \mathrm{~T} 8$ in the TOPOS TTD collection (Alexandrov et al., 2011), i.e. as a net with two topologically different nodes of coordination 3. Since the structure of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ contains four non-equivalent Sb atoms, this fact indicates a topological supersymmetry in the antimony sublattice. Indeed, applying the Systre routine (Delgado-Friedrichs \& O'Keeffe, 2003), the maximum symmetry $P 4_{1} 32$ was found for the $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ underlying net (that hence is chiral), and the number of non-equivalent Sb atoms was reduced to 2 .

According to the TOPOS TTO database (Alexandrov et al., 2011), the $3,3 \mathrm{~T} 8$ topology has been found in only one structure, a metal-organic copper(II) complex (Clegg et al., 2006) with the cubic symmetry $P 2_{1} 3$, which is a maximal translationequivalent subgroup of $P 4_{1} 32$. To search for inorganic structures with the 3,3T8 underlying net we analysed using TOPOS all 6229 structure types from the ICSD (release 2011/1). The $3,3 \mathrm{~T} 8$ topology was found only for the polyanion $\left[\mathrm{Si}_{4} \mathrm{O}_{4} \mathrm{~N}_{6}\right]^{10-}$ that occurred in the $\mathrm{Ce}_{4}\left(\mathrm{Si}_{4} \mathrm{O}_{4} \mathrm{~N}_{6}\right) \mathrm{O}$ structure type, also of the $P 2_{1} 3$ symmetry (Irran et al., 2000). The polyanion shows a very similar structure compared with $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ : the $\mathrm{Si}-\mathrm{N}-\mathrm{Si}$ links are topologically equivalent to the $\mathrm{Sb}-\mathrm{O}-\mathrm{Sb}$ ones, while the terminal O atoms of the $\mathrm{SiON}_{3}$ tetrahedra play the stereochemical role of the $E$ pairs in $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$, i.e. the correspondence $\left[\mathrm{Sb}_{4} E_{4} \mathrm{O}_{6}\right] \leftrightarrow\left[\mathrm{Si}_{4} \mathrm{O}_{4} \mathrm{~N}_{6}\right]^{10-}$ can be established.


Figure 7
Twisted $\mathrm{Sb}_{3} \mathrm{O}_{3}$ ring and connected $\mathrm{Sb}(4) \mathrm{O}_{3}$ trigonal pyramid as the basic building unit of the chains (see Fig. 6) in the crystal structure of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ in $P 2_{1} 2_{1} 2_{1}$ at ambient conditions in a perspective view. The connections to neighboring chains are indicated by dashed lines.

Nonetheless, $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ is the first case where the $3,3 \mathrm{~T} 8$ underlying net describes the whole structure topology.

The 3,3T8 underlying net can be more simplified if one considers the cyclic SBUs as a whole by representing them as their centres of gravity. The resulting net (Fig. 8 middle) is uninodal (with one topologically non-equivalent node), is


Figure 8
$\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ underlying net of the $3,3 \mathrm{~T} 8$ topology $(a)$, the corresponding srs net $(b)$, and the srs net in the most symmetric $\left(I 4_{1} 32\right)$ embedding $(c)$. The positions of the magenta balls coincide with the centres of gravity of the triangular SBUs.

Table 3
Bond-valence sums for $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ (with and without consideration of van der Waals radii).

| Atoms | Sb1 | Sb2 | Sb3 | Sb4 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Bond-valence sum $\dagger$ | 2.36 | 2.92 | 2.22 | 2.39 |  |  |
| Bond-valence sum $\ddagger$ | 2.64 | 3.28 | 2.61 | 2.66 |  |  |
| Atoms | O1 | O2 | O3 | O4 | O5 | O6 |
| Bond-valence sum $\dagger$ | 1.63 | 1.77 | 1.49 | 1.82 | 1.50 | 1.59 |
| Bond-valence sum $\ddagger$ | 1.90 | 2.00 | 1.84 | 1.91 | 1.67 | 1.88 |

$\dagger$ Without van der Waals radii. $\ddagger$ With van-der-Waals-radii
called srs, and describes the Si net in $\alpha-\mathrm{SrSi}_{2}$ (Fig. 8 bottom) as well as many other topological motifs of different chemical natures (Hyde et al., 2008). Thus, the 3,3T8 net can be described as a 'half-augmented' srs, i.e. the srs net where half of the nodes are augmented with triangles.

Considering the next three longer $\mathrm{Sb}-\mathrm{O}$ distances up to $3.35 \AA$ (which is still shorter as the sum of the van der Waals radii of $2.06+1.52 \AA$ ), additional stabilization of the crystal


Figure 9
Voronoi polyhedra for Sb atoms in the antimony sublattice: (a) Sb 1 in $\alpha$ $\mathrm{Sb}_{2} \mathrm{O}_{3}$ and Sb 1 in $\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}$; (b) Sb 1 and Sb 2 , and (c) Sb 3 and Sb 4 in $\gamma$ $\mathrm{Sb}_{2} \mathrm{O}_{3} .12$ grey Sb atoms form a distorted cuboctahedral environment; yellow distant Sb atoms give rise to additional minor faces of the Voronoi polyhedra due to the sublattice distortion. This figure is in colour in the electronic version of this paper.

Table 4
Overview of the motives of the mutual allocation, the effective coordination number (ECON), and the mean fictive ionic radii (MEFIR; $\mathrm{pm})$ for the three modifications of $\mathrm{Sb}_{2} \mathrm{O}_{3}$.

|  |  |  |  |  | ECoN |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\alpha-\mathrm{Sb}_{2} \mathrm{O}_{3}$ |  |  |  |  | MEFIR |
| O | Sb |  |  | 2.0 | 140 |
| ECoN | $3 / 2$ |  |  |  |  |
| MEFIR | 5.0 |  |  |  |  |
| $\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}$ |  |  |  |  |  |
| O 1 | Sb |  |  |  |  |
| O 2 | $1 / 2$ |  |  |  | 2.2 |
| ECoN | $2 / 2$ |  |  |  | 144 |
| MEFIR | 59 |  |  |  |  |
|  |  |  |  |  |  |
| $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ |  |  |  |  |  |
|  | Sb 1 | Sb 2 | Sb 3 | Sb 4 |  |
| O 1 | $1 / 1$ | $1 / 1$ | - | - | 1.4 |
| O 2 | $1 / 1$ | - | $1 / 1$ | - | 2.0 |
| O 3 | - | - | $1 / 1$ | $1 / 1$ | 2.2 |
| O 4 | - | $1 / 1$ | $1 / 1$ | - | 2.0 |
| O5 | $1 / 1$ | - | - | $1 / 1$ | 1.9 |
| O6 | - | $1 / 1$ | - | $1 / 1$ | 1.9 |
| ECoN | 2.3 | 2.8 | 3.2 | 3.1 |  |
| MEFIR | 51 | 49 | 65 | 62 |  |

structure of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ is achieved due to the contribution of these bonds to the bond-valence sum (Sidey, 2010) of the participating antimony-oxygen atoms (Table 3).

The crystal structures of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ and $\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}$ show similarities in the sense that in $\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}$ linked $\mathrm{Sb}_{2} \mathrm{O}_{3}$ units form infinite chains along the $c$ axis. Parallel chains in $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ are arranged in tetragonal rod packing (O'Keeffe \& Andersson, 1977), in contrast to $\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}$ where hexagonal rod packing is realised (Fig. 2). Both crystal structures are related via $P 2_{1} 2_{1} 2$ as an intermediate space group, allowing primary and secondary distortion modes.

An important similarity between all $\mathrm{Sb}_{2} \mathrm{O}_{3}$ modifications is that the Sb atoms form a distorted face-centered cubic sublattice. This is evident from the analysis of their Voronoi polyhedra (Fig. 9), which show a distinct cuboctahedral environment; the resulting 12 -coordinated net has the fcu (face-centered cubic) topology. Thus, the phase transitions keep the Sb motif topologically the same; the changes mainly consist of geometrical distortions and shifts of O atoms.

The motifs of the mutual allocation, the effective coordination number ( ECoN ) and the median fictive ionic radii (MEFIR; Hoppe, 1979) were calculated for all three polymorphs of $\mathrm{Sb}_{2} \mathrm{O}_{3}$ (Table 4). They are quite similar for O and Sb atoms. The Madelung fraction of the lattice energy (Hoppe, $1970 a, b)$ is of the same order of magnitude for identical ions. The Coulomb fraction of the lattice energy is very similar for all three modifications of $\mathrm{Sb}_{2} \mathrm{O}_{3}$, whereas the energy of the high-pressure phase lies between the values of the known phases (Table 5). The slightly higher value for the lattice energy in the case of $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ compared with $\alpha-\mathrm{Sb}_{2} \mathrm{O}_{3}$ can be understood by the shorter $\mathrm{Sb}-\mathrm{O}$ distances in the high-pressure phase.

Table 5
Comparison of the MAPLE values $\left(\mathrm{kJ} \mathrm{mol}^{-1}\right)$ for the three modifications of $\mathrm{Sb}_{2} \mathrm{O}_{3}$.

| Atom | MAPLE $\left(\alpha-\mathrm{Sb}_{2} \mathrm{O}_{3}\right)$ | $\operatorname{MAPLE}\left(\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}\right)$ | $\operatorname{MAPLE}\left(\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}\right)$ |
| :--- | :--- | :--- | :--- |
| Sb1 | $2318.7(4 \times)$ | $2284.0(4 \times)$ | 2169.6 |
| Sb2 | - | - | 2370.0 |
| Sb3 | - | - | 2186.1 |
| Sb4 | - | - | 2250.5 |
| O1 | $942.5(6 \times)$ | $1052.5(2 \times)$ | 1039.7 |
| O2 | - | $945.3(4 \times)$ | 1096.4 |
| O3 | - | - | 1019.3 |
| O4 | - | - | 951.9 |
| O5 | - | - | 939.8 |
| O6 | - | - | 988.3 |
|  | $\Sigma=14930 \mathrm{~kJ} \mathrm{~mol}^{-1}$ | $\Sigma=15022 \mathrm{~kJ} \mathrm{~mol}^{-1}$ | $\Sigma=15012 \mathrm{~kJ} \mathrm{~mol}^{-1}$ |

Table 6
Comparison of the volumes for the three modifications of $\mathrm{Sb}_{2} \mathrm{O}_{3}$.

|  | $\alpha-\mathrm{Sb}_{2} \mathrm{O}_{3}$ | $\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}$ | $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ |
| :--- | :--- | :--- | :--- |
| Unit cell volume $\left(\AA^{3}\right)$ | 1386.91 | 331.27 | 658.61 |
| Volume per formula unit $\left(\AA^{3}\right)$ | 86.68 | 82.82 | 82.33 |
| Molecular volume $\left(\mathrm{cm}^{3} \mathrm{~mol}^{-1}\right)$ | 52.21 | 49.88 | 49.59 |

Comparing the unit cell and the molecular volumes of all three $\mathrm{Sb}_{2} \mathrm{O}_{3}$ phases, it is clearly seen that the $\gamma$-phase possesses the smallest volume of the three modifications, as is expected for a high-pressure phase (Table 6). Whereas the volume of $\beta-\mathrm{Sb}_{2} \mathrm{O}_{3}$ is only about $0.6 \%$ larger than that of $\gamma$ $\mathrm{Sb}_{2} \mathrm{O}_{3}$, the difference between the $\beta$ and $\alpha$ phases is $\sim 4.6 \%$.

Other $A_{2} X_{3}$ structures like $\mathrm{Sb}_{2} \mathrm{~S}_{3}$ (Hofmann, 1933; Bayliss \& Nowacki, 1972) show similarities with $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$. The structure of $\mathrm{Sb}_{2} \mathrm{~S}_{3}$ is built by infinite columns of $\mathrm{Sb}_{4} \mathrm{~S}_{6}$ units along the $b$ axis. Despite the infinite chains the main difference to $\gamma-\mathrm{Sb}_{2} \mathrm{O}_{3}$ is that the chains are not directly connected to each other. The columns form sheets perpendicular to the $a$ axis with interatomic distances of $3.167 \AA$. These sheets again are held together by interatomic bonds between 3.373 and $3.642 \AA$, which are all considerably shorter than the van der Waals radii sum for Sb and S of $4.05 \AA$. High-pressure data of $\mathrm{Sb}_{2} \mathrm{~S}_{3}$ up to $p=10 \mathrm{GPa}$ in a diamond-anvil cell only revealed a change of the coordination polyhedra of the two Sb atoms with increasing pressure but no phase transition (Lundegaard et al., 2003). The high-pressure coordination of $\mathrm{Sb}_{2} \mathrm{~S}_{3}$ resembled more the coordination of $\mathrm{Bi}_{2} \mathrm{~S}_{3}$ at ambient pressure.

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## References

Alexandrov, E. V., Blatov, V. A., Kochetkov, A. V. \& Proserpio, D. M. (2011). CrystEngComm, 13, 3947-3958.

Amador, J., Gutierrez Puebla, E., Monge, M. A., Rasines, I. \& Ruiz Valero, C. (1988). Inorg. Chem. 27, 1367-1370.

Bayliss, P. \& Nowacki, W. (1972). Z. Kristallogr. 135, 308-315.
Blatov, V. A. (2006). IUCr CompComm Newsl. 7, 4-38, http:// www.topos.ssu.samara.ru.
Bozorth, R. M. (1923). J. Am. Chem. Soc. 45, 1621-1627.
Bruker (2007). TOPAS, Version 4.1. Bruker AXS, Karlsruhe, Germany.
Cheary, R. W., Coelho, A. A. \& Cline, J. P. (2004). J. Res. Natl. Inst. Stand. Technol. 109, 1-25.
Clegg, J. K., Lindoy, L. F., Mcmurtrie, J. C. \& Schilter, D. (2006). Dalton Trans. pp. 3114-3121.
Coelho, A. A. (2000). J. Appl. Cryst. 33, 899-908.
Coelho, A. A. (2003). J. Appl. Cryst. 36, 86-95.
Crystal Impact GbR (2000-2006). Endeavour, Version 1.4. Crystal Impact GbR, Bonn, Germany.
Debray, H. (1866). J. Prakt. Chem. 98, 151-153.
Dehlinger, U. (1927). Z. Kristallogr. 66, 108-119.
Dehlinger, U. \& Glocker, R. (1927). Z. Anorg. Allg. Chem. 165, 4145.

Delgado-Friedrichs, O. \& O'Keeffe, M. (2003). Acta Cryst. A59, 351360, http://www.gavrog.org.
Dihlström, K. (1938). Z. Anorg. Allg. Chem. 239, 57-64.
Dinnebier, R. E., Carlson, S., Hanfland, M. \& Jansen, M. (2003). Am. Mineral. 88, 996-1002.
Fenwick, F. \& Roberts, J. (1928). J. Am. Chem. Soc. 50, 2125-2147.
Ghedia, S., Locherer, T., Dinnebier, R. E., Prasad, D. L. V. K., Wedig, U., Jansen, M. \& Senyshyn, A. (2010). Phys. Rev. B, 82, 024106.

Gopalakrishnan, P. S. \& Manohar, H. (1975). J. Solid State Chem. 15, 61-67.
Hendricks, S. B. \& Burger, M. J. (1937). J. Chem. Phys. 5, 600.
Hofmann, W. (1933). Z. Kristallogr. 86, 225-245.
Hoppe, R. (1970a). Angew. Chem. 82, 7-16.
Hoppe, R. (1970b). Angew. Chem. Int. Ed. Engl. 9, 25-34.
Hoppe, R. (1979). Z. Kristallogr. 150, 23-52.
Hundt, R., Schön, J. C. \& Jansen, M. (2006). J. Appl. Cryst. 39, 6-16.
Hyde, S. T., O'Keeffe, M. \& Proserpio, D. M. (2008). Angew. Chem. Int. Ed. 47, 7996-8000.
Irran, E., Koellisch, K., Leoni, S., Nesper, R., Henry, P. F., Weller, M. T. \& Schnick, W. (2000). Chem. Eur. J. 6, 2714-2720.

Jansen, M. (1978). Angew. Chem. 90, 141-142.
Jansen, M. (1979). Acta Cryst. B35, 539-542.
LeBail, A., Duroy, H. \& Fourquet, J. L. (1988). Mater. Res. Bull. 23, 447-452.
Lundegaard, L. F., Miletich, R., Balic Zunic, T. \& Makovicky, E. (2003). Phys. Chem. Miner. 30, 463-468.

O'Keeffe, M. \& Andersson, S. (1977). Acta Cryst. A33, 914-923.
Orosel, D., Leynaud, O., Balog, P. \& Jansen, M. (2004). J. Solid State Chem. 177, 1631-1638.
Pätzold, H., Strunz, H. \& Gründer, W. (1962). Neues Jahrb. Miner. Abh. 5, 93-98.
Putz, H., Schön, J. C. \& Jansen, M. (1999). J. Appl. Cryst. 32, $864-$ 870.

Rietveld, H. M. (1969). J. Appl. Cryst. 2, 65-71.
Sidey, V. (2010). Acta Cryst. B66, 307-314.
Sillen, L. G. (1941). Z. Kristallogr. 103, 274-290.
Spek, A. L. (2003). J. Appl. Cryst. 36, 7-13.
Stahl, K., Legros, J. P. \& Galy, J. (1992). Z. Kristallogr. 202, 99-107. Stephens, P. W. (1999). J. Appl. Cryst. 32, 281-289.
Stewart, D. J., Knop, O., Ayasse, C. \& Woodhams, F. D. W. (1972). Can. J. Chem. 50, 690-700.
Svensson, C. (1974). Acta Cryst. B30, 458-461.
Svensson, C. (1975). Acta Cryst. B31, 2016-2018.
Thornton, G. (1977). Acta Cryst. B33, 1271-1273.
White, W. B., Dachille, F. \& Roy, R. (1967). Z. Kristallogr. 125, 450458.


[^0]:    ${ }^{1}$ Supplementary data for this paper are available from the IUCr electronic archives (Reference: KD5053). Services for accessing these data are described at the back of the journal.

